



# Warrant



**Product**

# Equity Warrant



- Warrant Introduction
- Warrant Payoffs
- Valuation
- Example




# Equity Warrant

## Warrant Introduction

- An equity warrant gives the holder the right to purchase shares at a fixed price from a firm. It is an option on the common stock of a firm issued by the same firm.
- Warrants are in many ways similar to call options, but a few key differences distinguish them.
- Warrants tend to have longer durations than do exchange-traded call options.
- They are traded over the counter more often than on an exchange.
- Investors cannot write warrants like they can options.
- Warrants do not pay dividends or come with voting rights.
- When warrants are exercised, the company typically issues new shares at the exercise price to fill the order, resulting dilution of the share value.

# Equity Warrant

- 
- Investors are attracted to warrants as a means of leveraging their positions in a security.
  - Warrants provide investors a way to hedge risk or speculate. They can also be used to exploiting arbitrage opportunities.
  - Warrants are frequently attached to bonds or preferred stock as a sweetener, which can be used to enhance the yield of the bond and make them more attractive to potential buyers.
  - Most commonly issued warrants are often detachable, meaning that they can be separated from the bond and sold on the secondary market.
  - Wedded warrants are not detachable. The investor must surrender the bond or preferred stock in order to exercise it.
  - Naked Warrants are issued on their own.



# Equity Warrant

## Warrant Payoff

- If there were  $n$  shares outstanding and  $m$  warrants exercised, the dilution factor corresponding to the percentage of the firm value that is represented by the warrants is given by

$$\alpha = m / (m + n)$$

- The payoff of the warrant at  $T$  is given by

$$payoff = \frac{m}{m + n} \max(A - K, 0)$$

where

$A = V/m$  the asset price

$V$  the firm value



# Equity Warrant

## Valuation

- Warrants can be valued by the Black-Scholes model, but some modifications must be made to the parameters.
- The price of a warrant under the diluted Black-Scholes model is given by

$$W = \frac{m}{m + n} (Ae^{-qT} \Phi(d_1) - Ke^{-rT} \Phi(d_2))$$

where

$$d_{1,2} = \frac{\ln\left(\frac{A}{K}\right) + (r - q \pm 0.5\sigma T)}{\sigma\sqrt{T}}$$

r        the interest rate

q        the dividend yield




# Equity Warrant

## Valuation (Con't)

- Strictly speaking,  $A$  is the asset price of the firm and  $\sigma$  is the volatility of the firm (not stock). Both of them are not observable.
- For simplicity, people may use stock price and stock volatility to replace the firm value  $A$  and the firm volatility  $\sigma$  above, although this simplification generally underestimates the warrant's price.

# Equity Warrant

- 
- There are several assumptions in this simplified warrant mode.
  - The price process of the stock follows a geometric Brownian motions.
  - The stock provides a continuous dividend
  - The risk-free interest rate is deterministic.
  - The volatility is constant.
  - The asset value per share is equal to the stock price.
  - The volatility of the firm is equal to the volatility of the stock.





# Equity Warrant

## Example

|                           |           |
|---------------------------|-----------|
| <b>Outstanding Shares</b> | 109254024 |
| <b>Underlying equity</b>  | BTX.A     |
| <b>Currency</b>           | USD       |
| <b>Strike</b>             | 4.55      |
| <b>Maturity Date</b>      | 10/1/2018 |
| <b>CallPut</b>            | Call      |
| <b>Exercise Type</b>      | European  |
| <b>Settlement Type</b>    | Physical  |
| <b>Position</b>           | 2038      |



Reference:

<https://finpricing.com/lib/EqWarrant.html>